

SOLVING TRIG EQUATIONS

$$2\sin^2 x + 5\sin x - 3 = 0$$

$$[0, 2\pi)$$

$$(2\sin x - 1)(\sin x + 3) = 0$$

$$2x^2 + 5x - 3 = 0$$

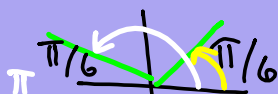
$$(2x - 1)(x + 3)$$

$$2\sin x - 1 = 0$$

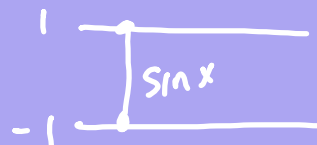
$$\sin x + 3 = 0$$

$$\sin x = \frac{1}{2}$$

$$\sin x = -3$$



$$\frac{\pi}{6}, \frac{5\pi}{6}$$



$$\sec \theta = 2 \cos \theta + 1$$

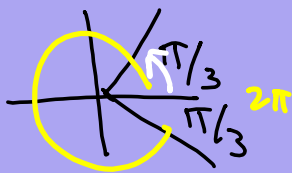
$$\cos \theta \left[\frac{1}{\cos \theta} = 2 \cos \theta + 1 \right]$$

$$1 = 2 \cos^2 \theta + \cos \theta$$

$$0 = 2 \cos^2 \theta + \cos \theta - 1$$

$$(2 \cos \theta - 1)(\cos \theta + 1) = 0$$

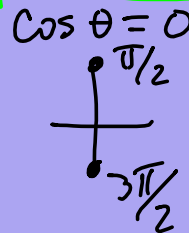
$$\cos \theta = \frac{1}{2} \quad \cos \theta = -1$$



$$\theta = \frac{\pi}{3}, \frac{5\pi}{3}, \pi$$

$[0, 2\pi)$

$$\theta \neq \frac{\pi}{2}, \frac{3\pi}{2}$$



(What if $(-\infty, \infty)$)

$$\frac{1}{-2} = 2 + \frac{3}{x+4}$$

Excluded values
 $x \neq 2, -4$

$(-\infty, \infty)$

$$\frac{\pi}{3} \pm 2\pi n$$

$$\frac{5\pi}{3} \pm 2\pi n$$

$$\pi \pm 2\pi n$$

$$12 \cot^2 \theta - 5 \cot \theta - 3 = 0 \quad [0^\circ, 360^\circ)$$

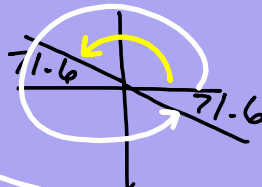
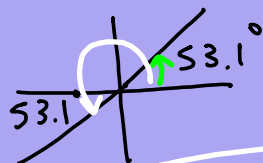
$$(4 \cot \theta - 3)(3 \cot \theta + 1) = 0$$

$$\cot \theta = \frac{3}{4} \quad \cot \theta = -\frac{1}{3}$$

$$\sin A = \frac{20}{37}$$

$$\sin^{-1}(20/37)$$

$$\cot^{-1}(3/4) = 53.1 \quad \cot^{-1}(1/3) = 71.6$$

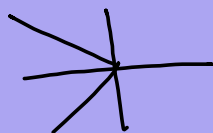


$$53.1^\circ, 233.1^\circ$$

$$108.9^\circ, 288.9^\circ$$

$$\cos \theta = -2/3$$

$$\cos^{-1}(-2/3) = 131.8^\circ$$



$$\sin^2 \theta + \cos \theta = 0$$

$$[0^\circ, 360^\circ)$$

$$1 - \cos^2 \theta + \cos \theta = 0$$

$$0 = \overset{a}{\downarrow} \cos^2 \theta - \overset{b}{\downarrow} \cos \theta - \overset{c}{\downarrow} 1$$

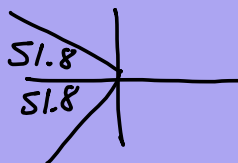
$$\cancel{(\cos \theta + 1)}(\cos \theta - 1)$$

$$\cos \theta = \frac{1 \pm \sqrt{1 - 4(1)(-1)}}{2(1)}$$

$$\cos \theta = \frac{1 \pm \sqrt{5}}{2}$$

$$\cos \theta = \cancel{1.618}$$

$$\cos \theta = -0.618$$



$$\theta = 128.2^\circ, 231.8^\circ$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\sin^2 \theta = 1 - \cos^2 \theta$$

$$x^2 + 2x - 5 = 0$$

$$x = \underline{\hspace{2cm}}$$