

SOLVING TRIG EQUATIONS

$$2\sin^2 x + 5\sin x - 3 = 0 \quad [0, 2\pi)$$

$$(2\sin x - 1)(\sin x + 3) = 0$$



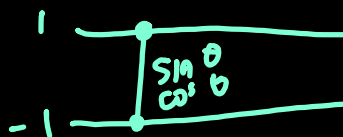
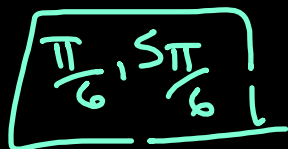
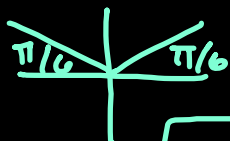
$$2\sin x - 1 = 0$$

$$\sin x = 1/2$$

$$\sin x + 3 = 0$$
~~$$\sin x = -3$$~~

$$2x^2 + 5x - 3 = 0$$

$$(2x - 1)(x + 3) = 0$$



$$\sec \theta = 2 \cos \theta + 1 \quad [0, 2\pi)$$

$$\cos \theta \left[\frac{1}{\cos \theta} = 2 \cos \theta + 1 \right]$$

$$1 = 2 \cos^2 \theta + \cos \theta$$

$$0 = 2 \cos^2 \theta + \cos \theta - 1$$

$$0 = (2 \cos \theta - 1)(\cos \theta + 1)$$

$$2 \cos \theta - 1 = 0$$

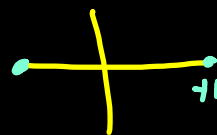
$$\cos \theta + 1 = 0$$

$$2 \cos \theta = \frac{1}{2}$$

$$\cos \theta = -1$$



$$\left[\frac{\pi}{3}, \frac{5\pi}{3}, \pi \right]$$



← check $\frac{1}{\cos \theta}$

$(-\infty, \infty)$

$$\frac{\pi}{3} \pm 2\pi n$$

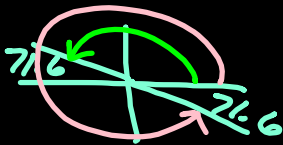
$$\frac{5\pi}{3} \pm 2\pi n$$

$$\pi \pm 2\pi n$$

$$12 \cot^2 \theta - 5 \cot \theta - 3 = 0 \quad [0^\circ, 360^\circ)$$

$$(3 \cot \theta + 1)(4 \cot \theta - 3) = 0$$

$$\cot \theta = -\frac{1}{3} \quad \cot \theta = \frac{3}{4}$$



$$108.4^\circ, 288.4^\circ, 53.1^\circ, 233.1^\circ$$

$$\sin^2 \theta + \cos \theta = 0 \quad [0^\circ, 360^\circ)$$

$$1 - \cos^2 \theta + \cos \theta = 0$$

$$6) \sin^2 \theta + \cos^2 \theta = 1$$

$$0 = \cos^2 \theta - \cos \theta - 1$$

$$x^2 - x - 1 = 0$$

$$0 = (\cos \theta - 1)(\cos \theta + 1)$$

$$\cos \theta = \frac{1 \pm \sqrt{1 + 4(1)(+1)}}{2(1)}$$

$$\cos \theta = \frac{1 \pm \sqrt{5}}{2}$$

~~$$\cos \theta = 1.618$$~~

$$\cos \theta = 0.618$$

$$\cos^{-1}(0.618)$$

$$\theta = 51.8^\circ, 308.2^\circ$$

