

LIMITS

What is
the y-coord.
approaching?

$$\lim_{x \rightarrow -6} f(x) = +\infty$$

$$\lim_{x \rightarrow -6^+} f(x) = -\infty$$

$$\lim_{x \rightarrow -6} f(x) = \text{DNE}$$

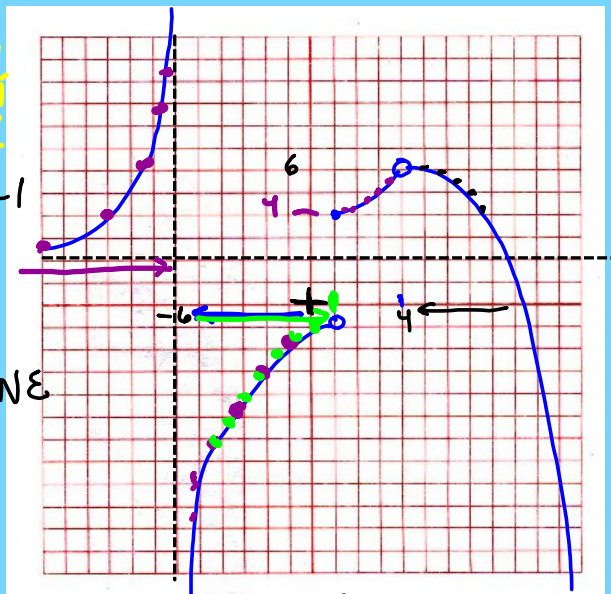
$$f(-6) = \text{undefined}$$

$$\lim_{x \rightarrow 1^-} f(x) = -1$$

$$\lim_{x \rightarrow 1^+} f(x) = 4$$

$$\lim_{x \rightarrow 1} f(x) = \text{DNE}$$

$$f(1) = 4$$



$$\lim_{x \rightarrow +\infty} f(x) = -\infty$$

$$\lim_{x \rightarrow -\infty} f(x) = 2$$

$$\lim_{x \rightarrow 4^-} f(x) = 6$$

$$\lim_{x \rightarrow 4^+} f(x) = 6$$

$$\lim_{x \rightarrow 4} f(x) = 6$$

$$f(4) = \text{undef.}$$

Draw a graph:

Domain: $[-5, \infty)$

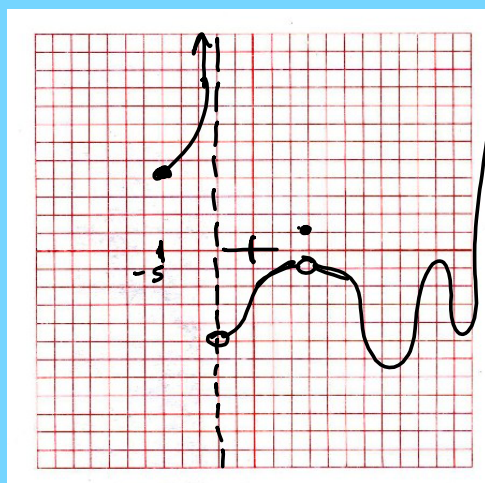
$f(-2) = \text{undef.}$ open circle or asymptote

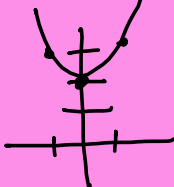
$f(3) = 1$ (3,1)

$\lim_{x \rightarrow -2^-} f(x) = +\infty$

$\lim_{x \rightarrow -2^+} f(x) = \text{DNE}$

$\lim_{x \rightarrow 3} f(x) = -1$



$$\lim_{x \rightarrow 1} x^2 + 2 = 3$$


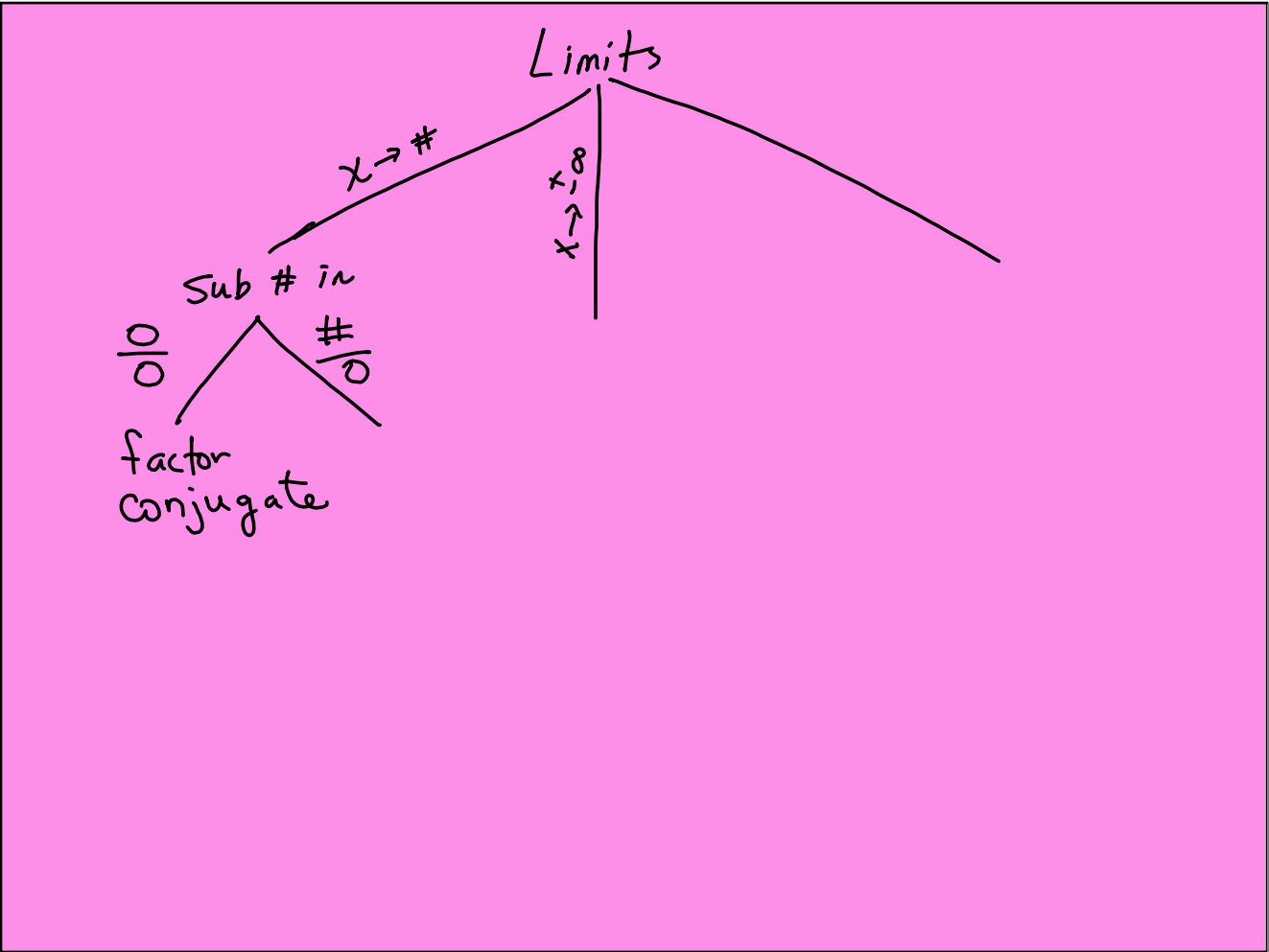
$$\lim_{x \rightarrow 2} \frac{3x^2 - 4x - 4}{x - 2} = \frac{0}{0}$$

← indeterminate form

$$\lim_{x \rightarrow 2} \frac{(3x+2)\cancel{(x-2)}}{\cancel{x-2}} = \boxed{8}$$

$$\lim_{x \rightarrow 3} \frac{x^2 - 4x + 3}{x^3 - 27} = \frac{0}{0}$$

$$\lim_{x \rightarrow 3} \frac{\cancel{(x-3)}(x-1)}{\cancel{(x-3)}(x^2 + 3x + 9)} = \frac{2}{27}$$



$$\lim_{h \rightarrow 0} \frac{\sqrt{9+h} - 3}{h} = \frac{3-3}{0} = \frac{0}{0}$$

$$\lim_{h \rightarrow 0} \frac{\cancel{9+h} - 9}{h(\sqrt{9+h} + 3)}$$

$$\lim_{h \rightarrow 0} \frac{\cancel{h}}{h(\sqrt{9+h} + 3)} = \frac{1}{3+3} = \left(\frac{1}{6}\right)$$