

# LINEAR FUNCTIONS

Function - Each x-coord is paired with EXACTLY ONE y-coord.

$\{(2,7) (3,-1) (4,8) (-9,6)\}$  yes

$\{(\underline{4},5) (6,-3) (7,-4) (\underline{4},11)\}$  No

$\{(\underline{8},-7) (\underline{-3},-7) (\underline{14},-7)\}$  yes

x's should not repeat!

\* What is a function?

\* Domain & Range

\* Function Notation

\* Lines

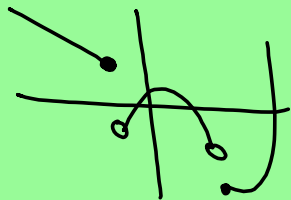
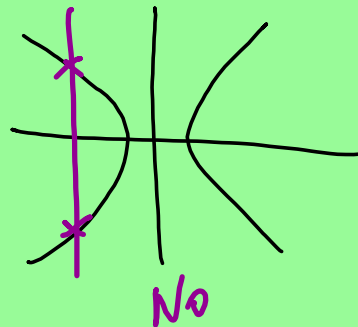
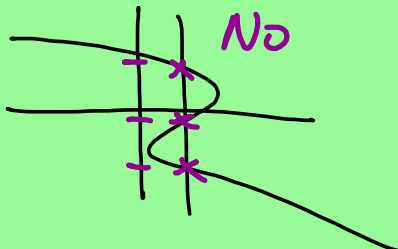
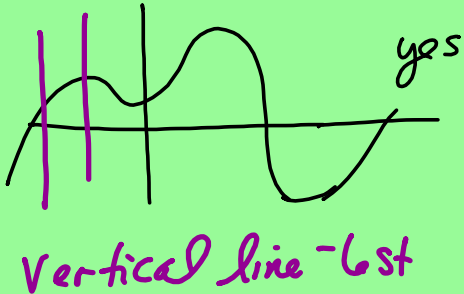
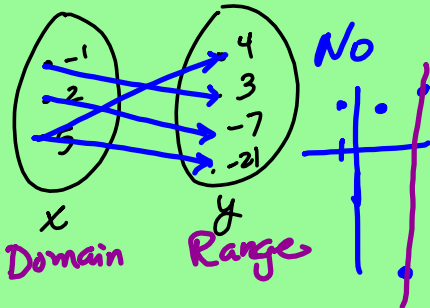
\* slope

\* Eq. of line

Mapping

Domain  
Set of  
x-coord

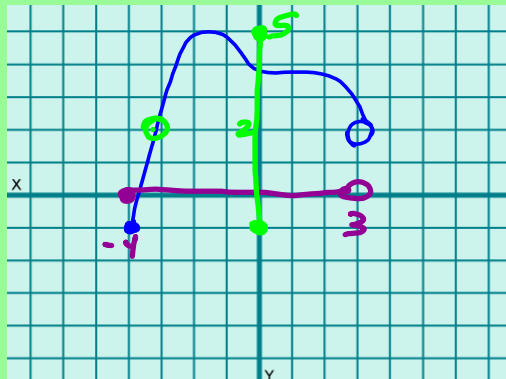
Range  
Set of  
y-word.



$$\{(-3, 4) (5, -8) (7, 2) (9, -5)\}$$

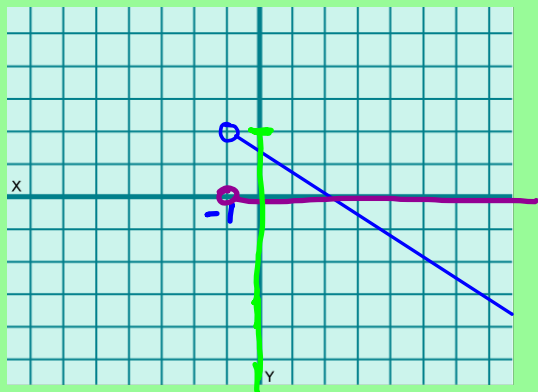
$$\text{Domain: } \{-3, 4, 5, 7\}$$

$$\text{Range: } \{-8, -5, 2, 4\}$$



$$\text{Domain: } -4 \leq x < 3$$

$$\text{Range: } -1 \leq y \leq 5$$



$$\text{Domain: } \text{L to R } x > -1$$

$$\text{Range: } \text{Low to High } y < 2$$

## FUNCTION NOTATION

$$f(x) = x^2 + 2x - 3$$

4 =

$$\text{Find } f(2) = (2)^2 + 2(2) - 3$$

$$= 4 + 4 - 3$$

$$= 5$$

$(2, 5)$

$$g(x) = \frac{3x-1}{x^2}$$

$$g\left(\frac{1}{2}\right) = \frac{3\left(\frac{1}{2}\right) - 1}{\left(\frac{1}{2}\right)^2}$$

$$= \frac{\frac{3}{2} - \frac{1}{2}}{\frac{1}{4}} = \frac{\frac{2}{2}}{\frac{1}{4}}$$

$$\frac{1}{2} \cdot \frac{4^2}{1} = \textcircled{2}$$

$$\left(\frac{1}{2}, 2\right)$$

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$$f(x) = \frac{x+1}{3} \quad D: \{-5, -1, \frac{1}{2}, 8\} \quad \text{Find range.}$$

$$f(-5) = \frac{-5+1}{3} = -\frac{4}{3}$$

$$R: \left\{-\frac{4}{3}, 0, \frac{1}{2}, 3\right\}$$

$$f(-1) = \frac{-1+1}{3} = 0$$

$$f\left(\frac{1}{2}\right) = \frac{\frac{1}{2}+1}{3} = \frac{\frac{3}{2}}{3} = \frac{3}{2} \cdot \frac{1}{3} = \frac{1}{2}$$

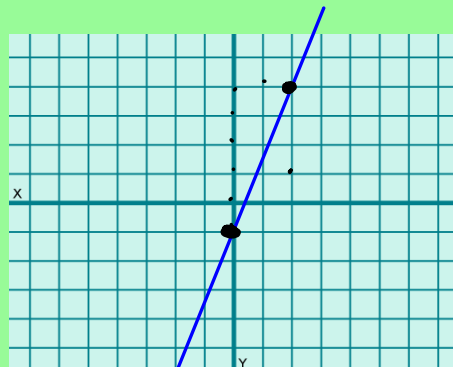
$$f(8) = \frac{8+1}{3} = 3$$

# LINES

$$\text{Slope} = \frac{\text{rise}}{\text{run}} = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$

$(2, -3)$   $(4, -9)$  Find slope.

$$m = \frac{-3 + 9}{2 - 4} = \frac{6}{-2} = -3$$



$$m = \frac{5}{2}$$

Babysitting

Kelly  
 flat fee \$10  
 \$6 per hour

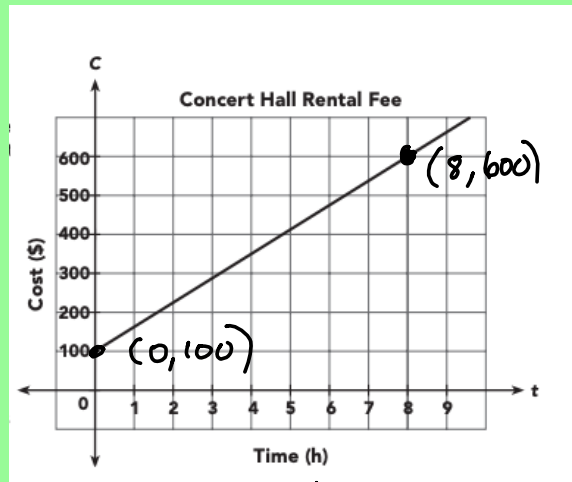
Kim

Hrs	\$
1	22
2	26
3	30
4	34

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{26 - 22}{2 - 1} = \frac{4}{1} = \$4 \text{ per hour}$$

Who charges more per hour?  
 Kelly

What is Kim's flat fee?  
 \$18



Flat fee? \$100

Hourly Rate:  $\frac{600 - 100}{8 - 0} = \frac{500}{8} = \$62.50$

Container P

$$m = \frac{1000 - 100}{0 - 60} = \frac{900}{-60} = -15 \frac{\text{mL}}{\text{min}}$$

$$y = mx + b \quad y = -15x + 1000$$

↑ slope    ↑ y-int

Container Q =  $\frac{800 - 200}{0 - 60} = \frac{600}{-60} = -10 \frac{\text{mL}}{\text{min}}$

$$y = -10x + 800$$

