

# SYSTEMS OF EQUATIONS REVIEW

1) Solve by graphing on calculator.

- a) Graph 2 lines      Standard form Menu-3-3-1-3  
 b) Intersect

f)  $3 \left[ \frac{1}{3}x + \frac{1}{3}y = 5 \right] \rightarrow x + y = 15$

## Substitution

$$5x - 2y = -29 \Rightarrow \frac{5x + 29}{2} = \frac{2y}{2}$$

$$3x + 4y = 19$$

$$\frac{5x + 29}{2} = y$$

$$3x + 4 \left( \frac{5x + 29}{2} \right) = 19$$

$$3x + 10x + 58 = 19$$

$$\frac{13x}{13} = \frac{-39}{13}$$

$$x = -3$$

$$y = \frac{5}{2}(-3) + \frac{29}{2}$$

$$= \frac{-15}{2} + \frac{29}{2}$$

$$= \frac{14}{2} = 7$$

$$\boxed{(-3, 7)}$$

Matrix Eq

$$6x - 4y = 33$$

$$3x + 5y = -33$$

~~[A]~~ [A]!

$$\begin{bmatrix} 6 & -4 \\ 3 & 5 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 33 \\ -33 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \frac{1}{30+20} \begin{bmatrix} 5 & 1 \\ -3 & 6 \end{bmatrix} \cdot \begin{bmatrix} 33 \\ -33 \end{bmatrix}$$

$$= \frac{1}{33} \begin{bmatrix} 165 + -33 \\ -99 + 198 \end{bmatrix}$$

$$= \frac{1}{33} \begin{bmatrix} 132 \\ -297 \end{bmatrix}$$

$$= \begin{bmatrix} 4 \\ -9 \end{bmatrix} \quad \boxed{(4, -9)}$$

3/ Graph + Shade

Find where shaded regions intersect

4-5) Linear Prog.

3-Var. Elim

$$\begin{array}{l} 7 \cdot \\ 4 \cdot \end{array} \begin{array}{l} 2x - y + 7z = 99 \\ 3x + 7y - 2z = 128 \\ 5x - 6y + 9z = 77 \end{array}$$

Elim #1 + #2  
- Elim. same variable.

$$\begin{array}{r} 14x - 7y + 14z = 243 \\ 3x + 7y - 2z = 128 \\ \hline 17x + 47z = 371 \\ \begin{array}{r} -12x + 4y - 42z = -144 \\ 5x - 6y + 9z = 77 \\ \hline -7x - 33z = -67 \end{array} \end{array}$$

$$x = -\frac{73}{9} \leftarrow \begin{array}{l} \text{Changing} \\ \text{to } -8 \end{array}$$

$$4x + 2y - 3z = -1$$

$$7x - y + 4z = 17$$

$$3x - 6y + 2z = -3$$

CRAMER'S  
RULE

$$y = \frac{\begin{vmatrix} \textcircled{4} & \textcircled{-1} & \textcircled{-3} \\ 7 & 17 & 4 \\ 3 & -3 & 2 \end{vmatrix}}{\begin{vmatrix} 4 & 2 & -3 \\ 7 & -1 & 4 \\ 3 & -6 & 2 \end{vmatrix}} =$$

$$4 \begin{vmatrix} 17 & 4 \\ -3 & 2 \end{vmatrix} + 1 \begin{vmatrix} 7 & 4 \\ 3 & 2 \end{vmatrix} + (-3) \begin{vmatrix} 7 & 17 \\ 3 & -3 \end{vmatrix}$$

$$4(34 - 12) + 1(14 - 12) - 3(21 - 51)$$

$$184 + 2 + 2$$