

ASYMPTOTES

Vertical

$$\lim_{x \rightarrow \#} f(x) = \pm \infty$$

↑
Denom = 0

Horizontal

$$\lim_{x \rightarrow \pm \infty} f(x) = \#$$

$$f(x) = \frac{4x^3 - 3x^2 - 5}{2x^2 + x - 3}$$

Slant - numerator is one power higher than the denom

Curvilinear - numerator is two or more powers higher than the denom

Find with long division

$$\begin{array}{r}
 2x - \frac{5}{2} \\
 \hline
 2x^2 + x - 3 \overline{) 4x^3 - 3x^2 + 0x - 5} \\
 \underline{-4x^3 + 2x^2 + 6x} \\
 -5x^2 + 6x - 5 \\
 \underline{-5x^2} \\
 6x - 5
 \end{array}$$

$y = 2x - 5/2$

$$\lim_{x \rightarrow +\infty} f(x) = 3$$

$$\frac{\text{Horiz}}{y=3}$$

$$\lim_{x \rightarrow -2^-} f(x) = -\infty$$

$$\frac{\text{Vertical}}{x=-2}$$

$$\lim_{x \rightarrow -2^+} f(x) = +\infty$$

$$f(-5) = 1 \quad f(0) = -8 \quad f(2) = -1$$

$$f(3) = -3 \quad f(5) = 2 \quad f(7) = 6$$

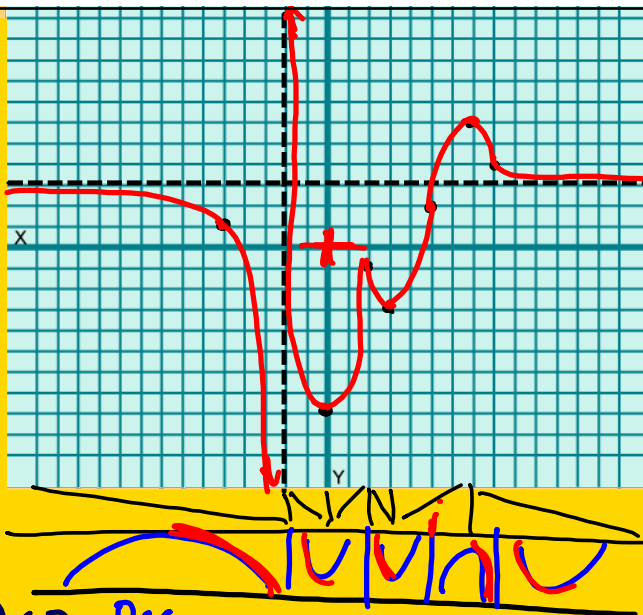
$$f(8) = 4 \leftarrow (8, 4)$$

$$(-\infty, -2) \quad (-2, 0) \quad (2, 3) \quad (7, \infty) \quad f'(x) < 0 \quad \text{Dec}$$

$$(0, 2) \quad (3, 7) \quad f'(x) > 0 \quad \text{Inc}$$

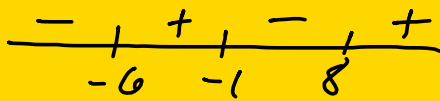
$$(-\infty, -2) \quad (5, 8) \quad f''(x) < 0$$

$$(-2, 2) \quad (2, 5) \quad (8, \infty) \quad f''(x) > 0$$



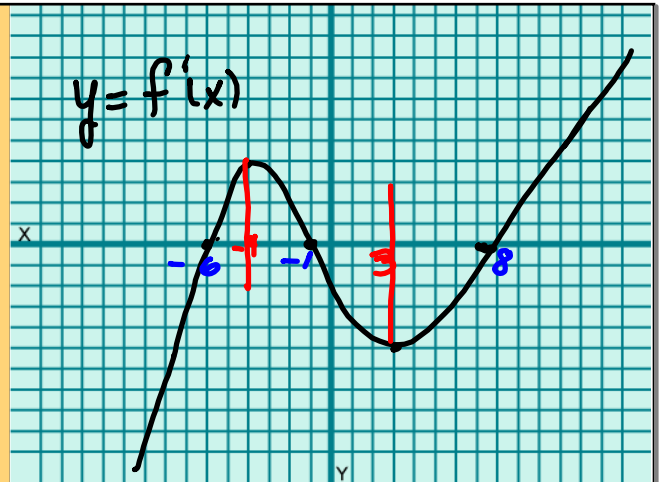
Crit pts where $f'(x) = 0$

Crit pts = -6, -1, 8

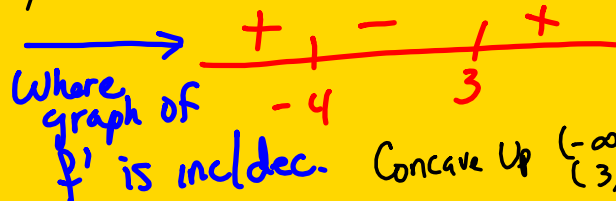


Inc/Dec Inc $f'(x) > 0$ +
 Dec $f'(x) < 0$ -
 where f' is above
 below x-axis

Inc $(-6, -1) (8, \infty)$
 Dec $(-\infty, -6) (-1, 8)$



Concavity
 Infl Pts. are the
 rel max/min on the
 f'



Where graph of f' is inc/dec.

Concave Up $(-\infty, -4)$
 $(3, \infty)$
 Concave Down $(-4, 3)$

