

MORE DISK METHOD

$$\pi \int_a^b (r_o^2 - r_i^2) dx$$

About $y = -3$

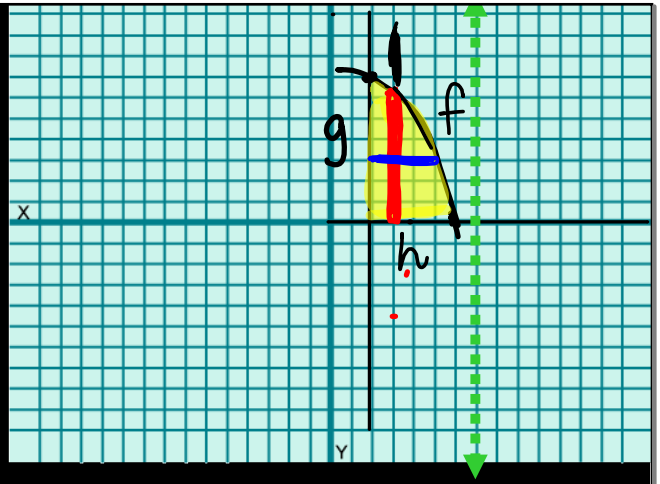
$$\pi \int_2^6 ((f+3)^2 - (h+3)^2) dx$$

About $y = 10$

$$\pi \int_2^6 ((10-h)^2 - (10-f)^2) dx$$

About $x = -5$

$$\pi \int_0^7 ((f-5)^2 - (g-5)^2) dy$$



About $x = 7$

$$\pi \int_0^7 (7-g)^2 - (7-f)^2 dy$$

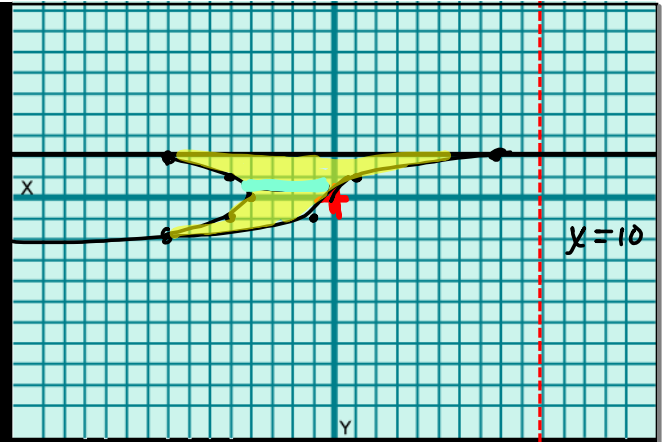
$$y^3 = \sqrt[3]{x}$$

$$y = \sqrt[3]{x} \quad y=2 \quad x=8$$

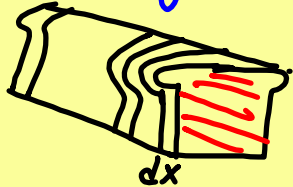
$$x = -y^2 - 4 \quad \text{about } x=10$$

$$\begin{array}{r|l} 0 & 0 \\ 1 & 1 \\ 8 & 2 \end{array}$$

$$\pi \int_{-2}^2 \left((10 - (-y^2 - 4))^2 - (10 - y^3)^2 \right) dy$$



Volume by Slicing



$$\int A(x) dx$$

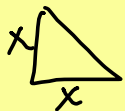
Base is formed by
 $y = x^2$ $y = 4$

Cross sections are squares.

$$A = s^2$$

$$\int_{-2}^2 (4 - x^2)^2 dx = \text{--- Units}^3$$

Isosceles Right Δ 's



$$A = \frac{1}{2}bh = \frac{1}{2}s \cdot s = \frac{1}{2}s^2$$

$$\frac{1}{2} \int_{-2}^2 (4 - x^2)^2 dx$$

Semi-circles

$$A = \frac{1}{2}\pi r^2$$

$$\frac{1}{2}\pi \left(\frac{4-x^2}{2}\right)^2$$

$$\frac{1}{2}\pi \int_{-2}^2 \left(\frac{4-x^2}{2}\right)^2 dx$$

Equilateral Δ .



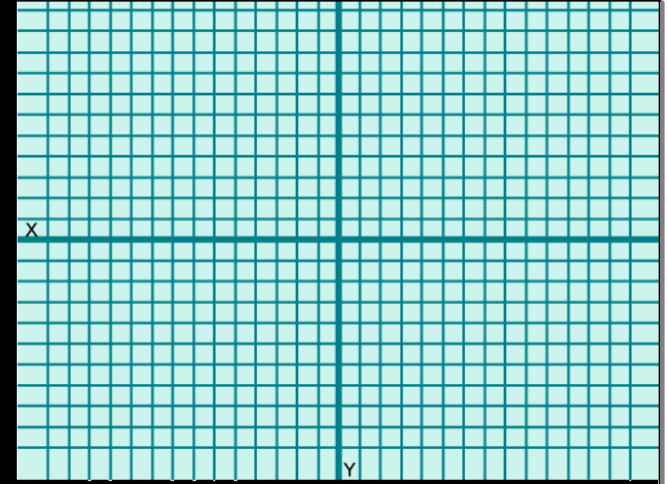
$$= \frac{1}{2} \cdot s \cdot \frac{\sqrt{3}}{2} s$$

$$A = \frac{\sqrt{3}}{4} s^2$$

Base

$$y = \sqrt[3]{x} \quad y = -\frac{1}{2}x + 6 \quad x = 0$$

Cross sections are
equilateral Δ 's



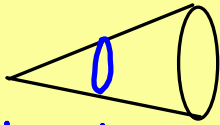
39/ nose cone of space
vehicle

$$r = \frac{1}{4}x^2$$

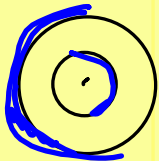
Circles

$$A = \pi r^2$$

$$\pi \int \left(\frac{1}{4}x^2\right)^2 dx$$



40/ annulus



Dam Video