

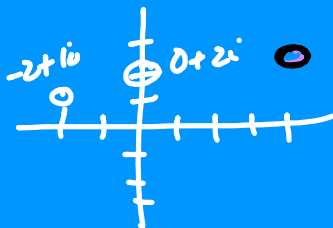
FRACTALS



Mandelbrot Set--Choose coordinate for c-value. Always iterate beginning with 0. Change coordinate for c-value each time you want to color a different point.

$$f(x) = x^2 + c \leftarrow$$

$f(c)$



Key Characteristics
Self-Similar

$$f(x) = x^2 + 4 + 2i$$

$$f(0) = 0^2 + 4 + 2i = 4 + 2i$$

$$f(4+2i) = (4+2i)^2 + 4 + 2i$$

$$= 16 + 16i + \cancel{4i^2} + 4 + 2i$$

$$= 16 + 18i$$

$$f(16+18i) = (16+18i)^2 + 4 + 2i$$

$$= 256 + 256i + \cancel{72i^2} + 4 + 2i$$

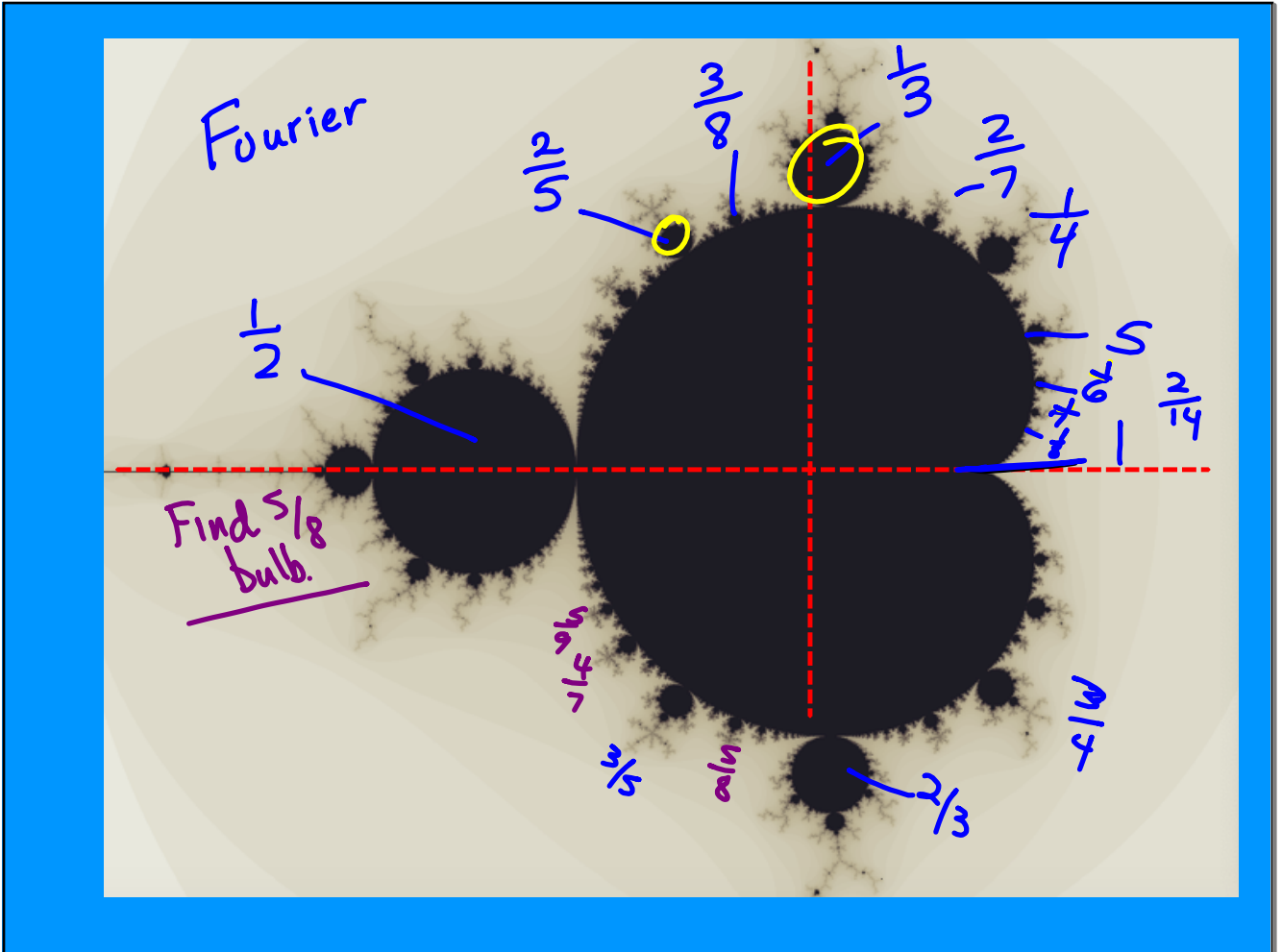
$$= 196 + 258i$$

$$\text{Orbit: } 4+2i, 16+18i, 196+258i$$

Calculator:

1) $x^2 + (1+i) \mid x = 0$

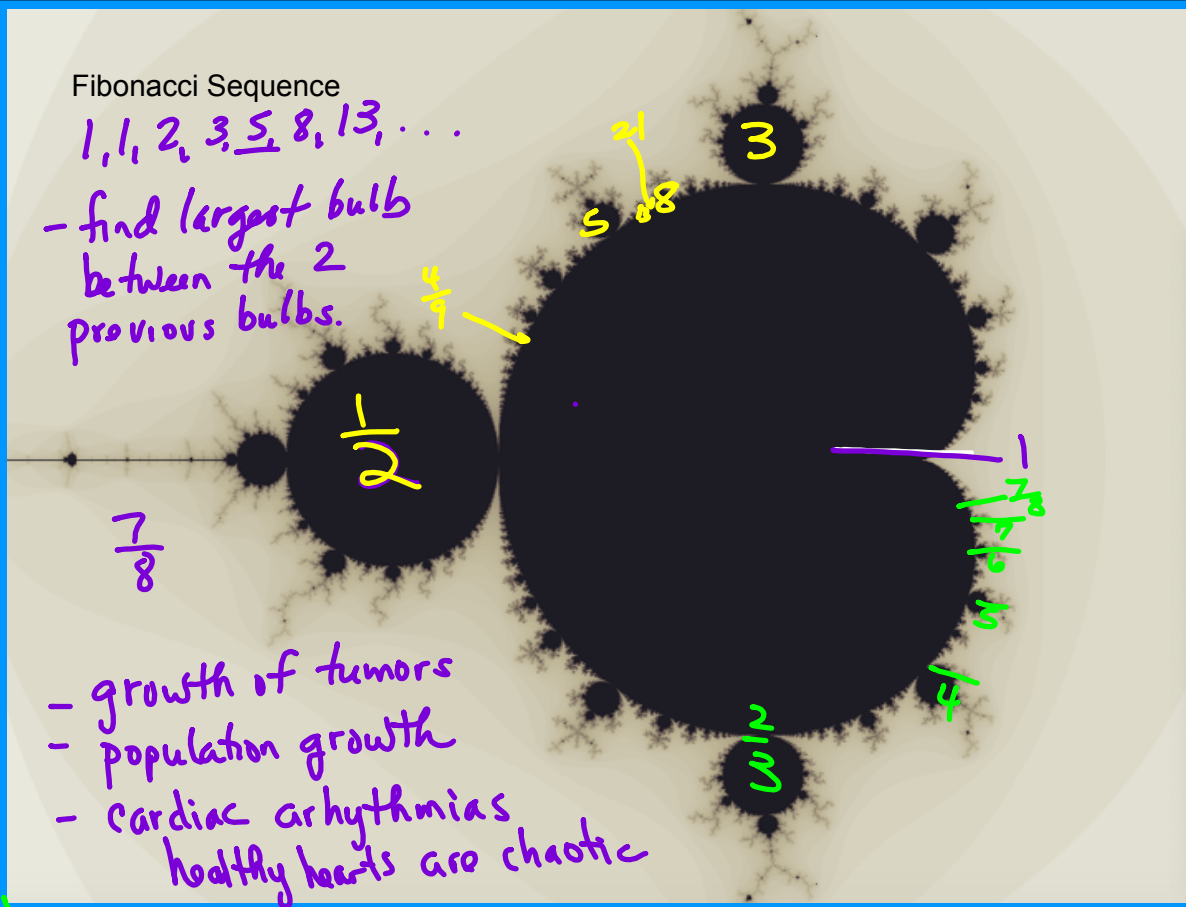
2) $x^2 + (1+i) \mid x = \text{Ans}$



Fibonacci Sequence

1, 1, 2, 3, 5, 8, 13, ...

- find largest bulb
between the 2
previous bulbs.

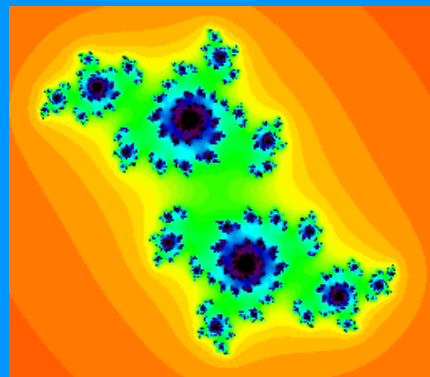
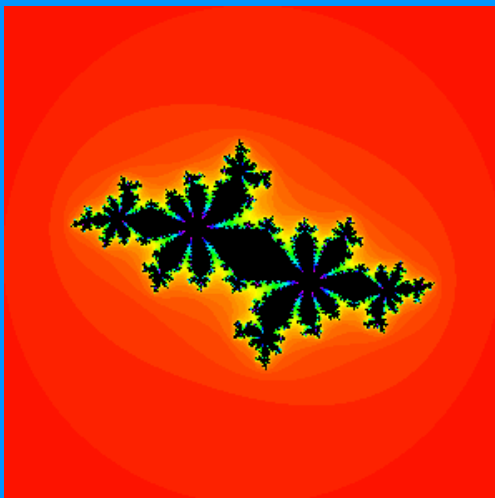
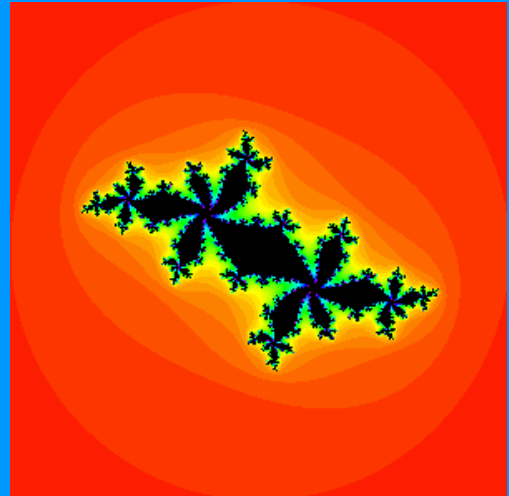
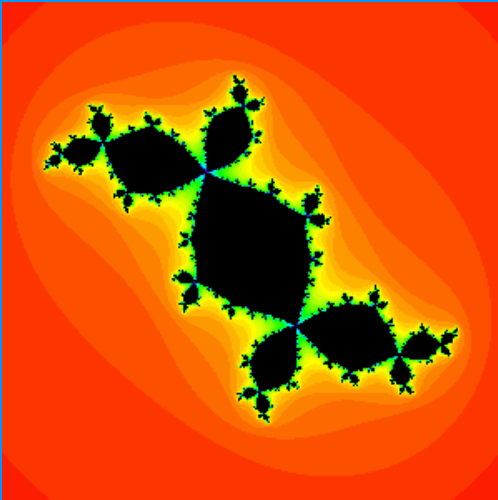


- growth of tumors
- population growth
- cardiac arrhythmias
healthy hearts are chaotic

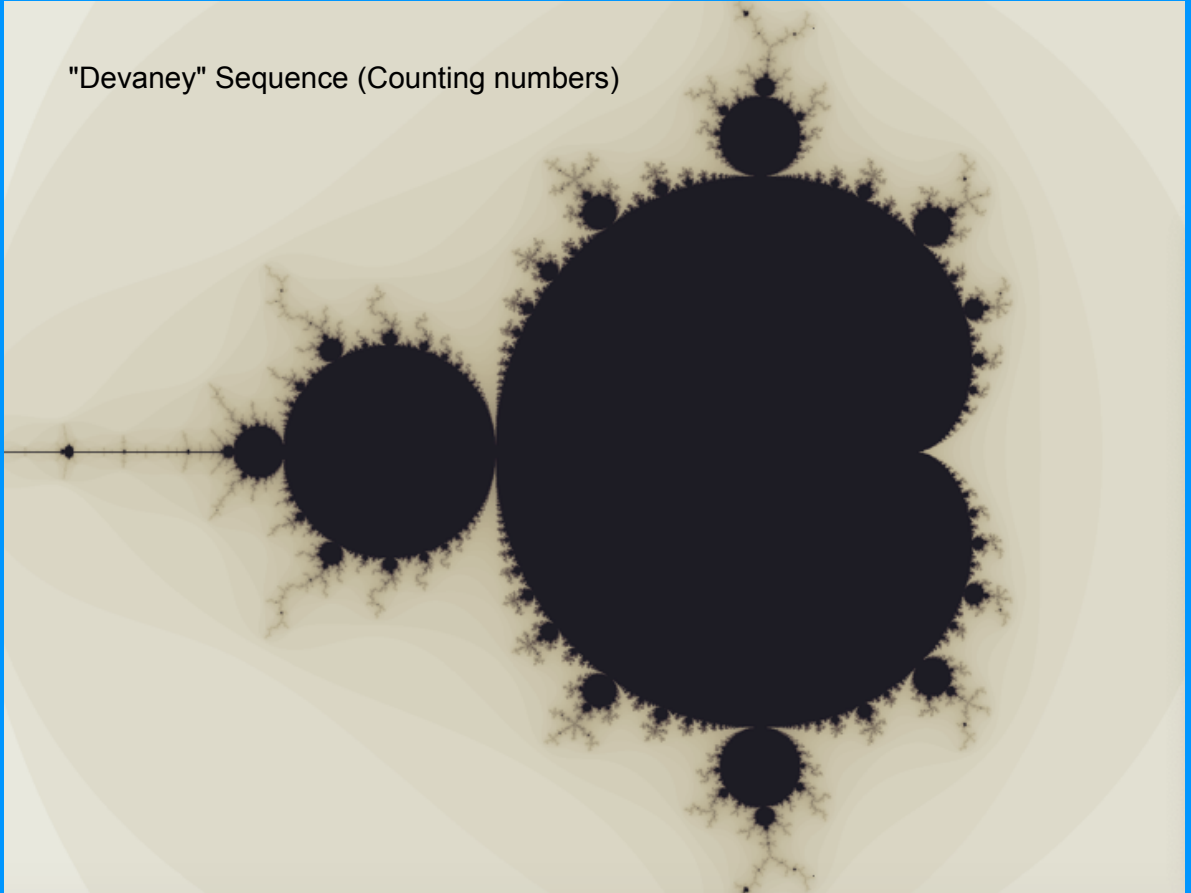
Julia Sets

Mandelbrot

Julia



"Devaney" Sequence (Counting numbers)



MORE DERIVATIVES

$$f(x) = 3x^7 \cdot 5x^4 = 15x^{11}$$



~~$$f(x) = 21x^6 \cdot 20x^3 = 420x^9$$~~

$$f'(x) = 165x^{10}$$

$$f(x) = 3x^7 \cdot 5x^4$$

$$f'(x) = 3x^7 \cdot 20x^3 + 5x^4 \cdot 21x^7$$

$$= 60x^{10} + 105x^{10}$$

$$= 165x^{10}$$

PRODUCT RULE

$$\frac{d}{dx} f \cdot g = f \cdot g' + g \cdot f'$$

1st · d'2nd + 2nd · d'1st

$$f(x) = (7x^5 + 3x^8 - 2) \left(8x - \frac{7}{\sqrt{x^2}} + 9 \right)$$

$$-7x^{-2/5}$$

$$f'(x) = \overset{1st}{(7x^5 + 3x^8 - 2)} \overset{d'2nd}{\left(8 + \frac{14}{5}x^{-7/5} \right)} + \overset{2nd}{\left(8x - 7x^{-2/5} + 9 \right)} \overset{d'1st}{(35x^4 + 24x^7)}$$

QUOTIENT RULE

$$\frac{d}{dx} \frac{f}{g} = \frac{g \cdot f' - f \cdot g'}{g^2}$$

$$= \frac{\text{low} \cdot \text{d'high} - \text{high} \cdot \text{d'low}}{\text{low}^2}$$

$$f(x) = \frac{1}{x} = x^{-1}$$

$$f'(x) = -1x^{-2} = -\frac{1}{x^2}$$

$$f(x) = \frac{x^4 - 7x^3 + 8}{2x^5 - 17x^2}$$

$$f'(x) = \frac{(2x^5 - 17x^2) \cdot (4x^3 - 21x^2) - (x^4 - 7x^3 + 8)(10x^4 - 34x)}{(2x^5 - 17x^2)^2}$$

CHAIN RULE

$$\frac{d}{dx} f[g(h(x))] = f'[g(h(x))] \cdot g'(h(x)) \cdot h'(x)$$

$$f(x) = \sin^4(\cos(3x^2-7)^5)$$

$$f(x) = (x^2 - 7x + 3)^8$$

$$f'(x) = 8(x^2 - 7x + 3)^7 \cdot (2x - 7)$$

$$f(x) = \sqrt{x^2 + 3 - 5(x^2 + 4)^9}$$

$$= [x^2 + 3 - 5(x^2 + 4)^9]^{1/2}$$

$$f'(x) = \frac{1}{2} [x^2 + 3 - 5(x^2 + 4)^9]^{-1/2} \cdot [2x - 45(x^2 + 4)^8 \cdot 2x]$$

$$f(x) = \frac{(x^5 - 4x^8 + 7)(3x^2 - 5x^7)}{(x^6 + 8)^{100}}$$

$$f'(x) = \frac{\overset{\text{low}}{(x^6 + 8)^{100}} \left[\overset{\text{1st}}{(x^5 - 4x^8 + 7)} \overset{\text{d'2nd}}{(6x - 85x^6)} + \overset{\text{2nd}}{(3x^2 - 5x^7)} \overset{\text{d'1st}}{(5x^4 - 32x^7)} \right]}{\overset{\text{d'high}}{(x^6 + 8)^{100}}}$$

$$\frac{\overset{\text{high}}{-(x^5 - 4x^8 + 7)(3x^2 - 5x^7)} - \overset{\text{d'low}}{100(x^6 + 8)^{99} \cdot (6x^5)}}{\left[(x^6 + 8)^{100} \right]^2}$$