

WELCOME TO CALCULUS!

Functions

$$x^3 + 3x^2 - 2x$$

$$f(x) = \frac{x+1}{x^2-9}$$

$$x \neq 3, -3$$

$$f(x) = \sqrt{\frac{x+7}{x-4}}$$

$$x \neq 4$$

$$\begin{array}{c} + \quad - \quad + \\ \text{min} \quad \text{max} \quad \text{min} \\ \hline 7 \quad 0 \quad 4 \end{array}$$

$$(-\infty; 7] \cup (4, \infty)$$

Domain

Polyn	$\mathbb{R} \quad (-\infty, \infty)$
Rational	Denom $\neq 0$
odd Root	$\mathbb{R} \quad (-\infty, \infty)$
Even Root	must contain + values Testing Pts.!

$$f(x) = \sqrt{x+2} \quad g(x) = \frac{2}{x-1}$$

$$(f \circ g)(x) = \sqrt{\frac{2}{x-1} + 2}$$

$$= \sqrt{\frac{2 + 2(x-1)}{x-1}}$$

$$= \sqrt{\frac{2 + 2x - 2}{x-1}}$$

$$= \sqrt{\frac{2x}{x-1}}$$

Domain:

- 1) Domain of f
- 2) Domain of g
- 3) Domain of $f \circ g$
- 4) Where do all 3 exist?

$$f: \text{---} \left[-2, \infty \right) \text{---}$$

$$g: x \neq 1 \text{ ---} \times \text{---}$$

$$f \circ g: \text{---} \left[-2, 0 \right] \cup \left(1, \infty \right) \text{---}$$

Combine all 3 domains:

$$\text{---} \left[-2, 0 \right] \cup \left(1, \infty \right) \text{---}$$

All 3 exist at:

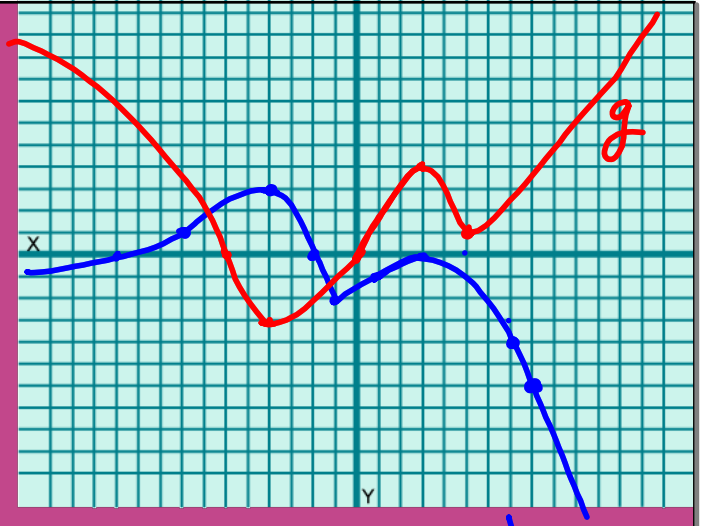
$$[-2, 0] \cup (1, \infty)$$

f = blue graph
 g = red graph

Find $(f \circ g)(5)$

$$g(5) = 1 \quad \begin{array}{c} \text{g} \\ \hline \text{When } x=5, \\ y=1 \end{array}$$

$$f(1) = -1 \quad \begin{array}{c} \text{f} \\ \hline \text{When } x=1 \\ y=-1 \end{array}$$



Find $(g \circ f)(8)$

$$f(8) = -6$$

$$g(-6) = 0$$