

## Day 1 Assignment

(a)  $f(x) = 4\cos x$ (b)  $f(x) = 2\sin x$ (c)  $f(x) = \frac{2}{x^2} + 3\sqrt{x}$ 

## Day 2 Assignment (Product, Quotient & Chain Rules)

Find f'(x) using the product, quotient or chain rules. 1.  $f(x) = (x^3 + 7x^2 - 8)(2x^{-3} + x^{-4})$ 2.  $f(x) = (\frac{1}{x} + \frac{1}{x^2})(3x^3 + 27)$ 3.  $f(x) = \frac{4x + 1}{x^2 - 5}$ 4.  $f(x) = (\frac{3x + 2}{x})(x^{-5} + 1)$ 5.  $f(x) = \frac{\sin x}{x^2 + \sin x}$ 6.  $f(x) = (x^2 + 1)\sec x$ 7.  $f(x) = \frac{\cot x}{1 + \csc x}$ 

(d) 
$$f(x) = (2x^2 + 3)(x^3 - 5)$$
  
(e)  $f(x) = \frac{4}{3x^5} - 6\sqrt[3]{x^2}$ 

8.  $f(x) = \sec x \tan x$ 

9.  $f(x) = \frac{\sin x \sec x}{1 + x \tan x}$ 

10.  $f(x) = \frac{(x^2 + 1)\cot x}{3 - \cos x \csc x}$ 

11.  $f(x) = (x^3 + 2x)^{37}$ .

13.  $f(x) = \sqrt{4 + \sqrt{3x}}$ 

 $f(x) = x^2 \cos x + 4 \sin x$ 

14. Find f''(x).

12.  $f(x) = \frac{4}{(3x^2 - 2x + 1)^3}$ 

(Quotient rule is not the easiest way.)

(f)  $f(x) = \tan x + \csc x$ (g)  $f(x) = 4\sin x - 3\cot x + 2$ (h)  $f(x) = \sin x (2\csc x - \cot x)$ Hint: Trig identities might be useful.

Find 
$$\frac{dy}{dx}$$
.  
15.  $y = (5x+8)^7 (1-\sqrt{x})^6$   
16.  $y = \left(\frac{x-5}{2x+1}\right)^3$   
17.  $y = \frac{(2x+3)^3}{(4x^2-1)^8}$ 

Write the equation of the line tangent to the given function at the given value of *x*.

18. 
$$y = \left(x - \frac{1}{x}\right)^3$$
,  $x = 2$   
19.  $y = x^2 \sqrt{5 - x^2}$ ,  $x = 1$ 

## Day 3 Assignment (More Chain Rule) Find f'(x)11. Solve with CAS: 6. $y = \frac{\sin(x^6)}{\sec(3x^2 + 5x^4)^8}$ $y = \tan^4 \left[ 2 + \frac{(7-x)\sqrt{3x^2+5}}{x^3 + \sin x} \right]$ 1. $f(x) = \sin\left(\frac{1}{r^2}\right)$ 7. $y = \sin(\tan 3x)^7$ 2. $f(x) = \tan^4(x^3)$ Write the equation of the line 8. $y = \cos^3(\sin 2x)$ tangent to the given function at the 3. $f(x) = \sqrt{3x - \sin^2(4x)}$ given value of *x*. 9. $y = [x + \sin^3(x^5)]^{12}$ 12. $y = x \cos 3x, x = \pi$ 4. $f(x) = \left[ x + \csc(x^3 + 3) \right]^{-3}$ 13. $y = \tan(4x^2), x = \sqrt{\pi}$ 10. $y = \left[\frac{x \sin 2x}{\tan^4(x^7)}\right]^5$ Find $\frac{dy}{dx}$ . 5. $y = x^5 \sec(\frac{1}{x})$

## **Differentials**

- 1. Find *dy* if  $y = \sqrt{3x 2}$  and *x* changes from 2 to 2.03. 2. Find *dA* if  $A = 3x^2 x$  and *x* changes from 4 to 4.1.
- 3. The radius of a round manhole cover is estimated to be 16 in., with a maximum error of  $\pm 0.06$  in. (a) Use differentials to estimate the maximum error in the area to the nearest hundredth. (b) Approximate the percentage error in the radius and the area to the nearest thousandth of a percent.
- 4. A spherical balloon is being inflated with gas. (a) Use differentials to approximate the increase in the volume if the diameter changes from 2 ft. to 2.02 ft. to the nearest hundredth. (b) Approximate the percentage error in the radius and the volume to the nearest percent.
- 5. A metal cube with sides of 15 in. is coated with a sealant 0.01 in thick. Approximate the change in the surface area to the nearest tenth.
- 6. A metal rod 18 cm long and 5 cm in diameter lies at the bottom of the ocean. It gradually develops a layer of corrosion 0.1 cm thick along its surface. Approximate the change in the volume to the nearest hundredth.