

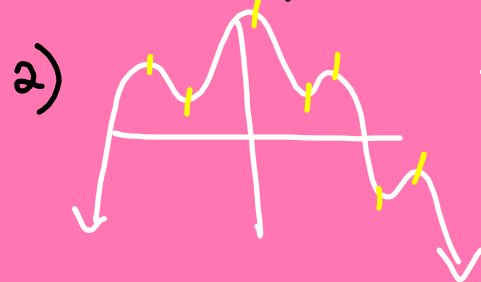
POLYNOMIAL + RATIONAL FUNCTIONS

$$f(x) = -3x^5 + 2x^4 - 6x^2 + 7x - 1$$



$$\lim_{x \rightarrow -\infty} f(x) = +\infty$$

$$\lim_{x \rightarrow +\infty} f(x) = -\infty$$



$$-x^8$$



3) Synthetic Division

$$d) 2x^4 + 5x^3 + 4x^2 - x - 10 = 0 \quad \pm 1 \pm 2 \pm 5 \pm 10$$

_____ | $x = \#$

$$\begin{array}{r|rrrrrr} 1 & 2 & 5 & 4 & -1 & -10 \\ & +0 & 2 & 7 & 11 & 10 \\ \hline & 2 & 7 & 11 & 10 & 0 \end{array}$$

$$(x-1)(2x^3 + 7x^2 + 11x + 10)$$

$$-16 + 28 - 22 + 10 = 0$$

$$\begin{array}{r|rrrr} -2 & 2 & 7 & 11 & 10 \\ & +0 & -4 & -6 & -10 \\ \hline & 2 & 3 & 5 & 0 \end{array}$$

$$(x-1)(x+2)(2x^2 + 3x + 5)$$

$$x=1 \quad x=-2$$

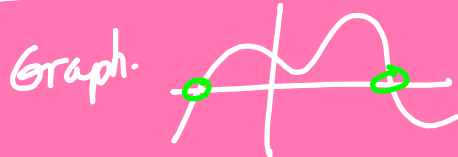
$$x = \frac{-3 \pm \sqrt{9 - 4(2)(5)}}{2(2)}$$

$$x = \frac{-3 \pm \sqrt{9 - 40}}{4}$$

$$= \frac{-3 \pm \sqrt{-31}}{4}$$

$$= \frac{-3 \pm i\sqrt{31}}{4}$$

4/ Zeros on calculator.



Menu-6-1

5) Roots: $-\frac{5}{3}, \pm 4i$

$$\curvearrowright x = -\frac{5}{3} \quad x = 4i \quad x = -4i$$

$$3x = -5$$

$$3x + 5 = 0$$

$$x - 4i = 0$$

$$x + 4i = 0$$

For $(3x+5)(x-4i)(x+4i)$

$$(3x+5)(x^2 + 16)$$

$$(3x+5)(x^2 + 16)$$

$$3x^3 + 5x^2 + 48x + 80 = 0$$

6 Rational Functions

* No Holes
b.c. d.
(x-1)
(x+2)

$$4 \left[\frac{3}{x-1} + \frac{2}{x+2} \right] \quad x \neq 1, -2$$

$$4(x-1)(x+2) = 3(x+2) + 2(x-1)$$

$$4 < \frac{3}{x-1} + \frac{2}{x+2}$$

- 1) Set < 0 or > 0
- 2) Make common denom.
- 3) Test Points

7) Partial Fractions 😊

8) Simplify.

$$\frac{4x(2x-3)^{-1/3} (4x+5)^{-3+4} - 20x^2(2x-3)^{2/3+5} (4x+5)^{-4}}{\left[(2x-3)^{2/3}\right]^2}$$

$$\frac{4x \cancel{(2x-3)^{-1/3}} \cdot \cancel{(4x+5)^{-4}} \left[4x+5 - 5x(2x-3)\right]}{(4x+5)^4 (2x-3)^{4/3+1/3}}$$

$$\frac{4x [4x+5 - 10x^2 + 15x]}{(4x+5)^4 (2x-3)^{5/3}}$$

$$\frac{4x [-10x^2 + 19x + 5]}{(4x+5)^4 (2x-3)^{5/3}}$$