

IDENTITIES REVIEW with

Sum & Product Identities

Purpose — to switch addition/subtraction of $\sin x / \cos$ functions to multiplication or vice versa.

$$\begin{aligned}\sin 40^\circ - \sin 100^\circ &= 2 \cos \left(\frac{40^\circ + 100^\circ}{2} \right) \sin \left(\frac{40^\circ - 100^\circ}{2} \right) \\ &= 2 \cos 70^\circ \sin (-30^\circ) \\ &= -2 \cos 70^\circ \sin 30^\circ\end{aligned}$$

Review

3

$$\cos 45^\circ \sin 25^\circ = \frac{1}{2} [\sin 70^\circ - \sin 20^\circ]$$

$$\begin{aligned}\frac{\equiv}{\equiv} & \frac{1}{2} [\sin(45^\circ + 25^\circ) - \sin(45^\circ - 25^\circ)] \\ \equiv & \frac{1}{2} [\sin 70^\circ - \sin 20^\circ]\end{aligned}$$

True

Test

6 T-F

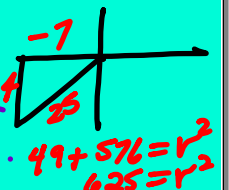
Write 8 fund. identities

11-14) Evaluate. - Use
2 or 3 specific
angle
values

15-20) Draw a picture problems
(A+B)

Verify = 4 problems

20/ Find $\cos\left(\frac{x}{2}\right)$

given $\cot x = \frac{1}{2} + \frac{x}{y}$ 
 x in $Q II$. $180^\circ < x < 270^\circ$
 $Q II = 90^\circ < \frac{x}{2} < 135^\circ$

$$\cos\left(\frac{x}{2}\right) = \pm \sqrt{\frac{1 + \cos x}{2}}$$

$$= - \sqrt{\frac{1 + \cos x}{2}}$$

$$= - \sqrt{\frac{1 + \frac{1}{25}}{2}}$$

$$= - \sqrt{\frac{\frac{25}{25} + \frac{1}{25}}{2}}$$

$$= - \sqrt{\frac{26}{50}}$$

$$= \boxed{-\frac{\sqrt{13}}{5}}$$

$$\begin{aligned} \cancel{21} \quad 4 \sin^2 \theta \cos^2 \theta &= 1 - \cos^2 2\theta \\ &= \sin^2(2\theta) \\ &= [2 \sin \theta \cos \theta]^2 \\ &= 4 \sin^2 \theta \cos^2 \theta \end{aligned}$$