

# SOLVING INEQUALITIES

$$2m+7 < 5m-9 \leq 3m+2$$

$$\begin{array}{l} 2m+7 < 5m-9 \\ -2m+9 \quad -2m \end{array} \quad \text{AND} \quad \begin{array}{l} 5m-9 \leq 3m+2 \\ -3m+9 \quad -3m+9 \end{array}$$

$$\frac{16}{3} < \frac{3m}{3}$$

$$\frac{2m}{2} \leq \frac{11}{2}$$

$$\frac{16}{3} < m \quad \text{AND} \quad m \leq \frac{11}{2}$$

BOTH



AND = OVERLAP

$$\boxed{\frac{16}{3} < m \leq \frac{11}{2}}$$

$$\begin{array}{l} -3 \leq 2y+9 \\ -9 \quad -9 \end{array} \quad \text{OR} \quad \begin{array}{l} 18-4y < -10 \\ -18 \quad -18 \end{array}$$

$$\begin{array}{l} -12 \leq 2y \\ -2 \quad -2 \end{array} \quad \begin{array}{l} -4y < -28 \\ -4 \quad -4 \end{array}$$

$$-6 \leq y \quad \text{OR} \quad y > 7$$

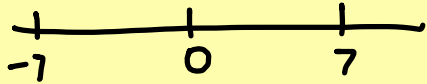


$$y \geq -6$$

OR = Anything Shaded

# ABSOLUTE VALUE

$$|-7| = 7$$



$$-2|x+2| + 12 = 0$$

$$\frac{-2|x+2|}{-2} = \frac{-12}{-2}$$

$$|x+2| = 6$$

$$x+2 = 6 \quad x+2 = -6$$

$$\boxed{x=4 \quad x=-8}$$

$$|x| = 4$$

$$x = -4 \text{ or } x = 4$$

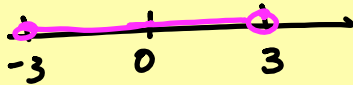
$$|K+6| = 3$$

$$K+6 = 3 \quad K+6 = -3$$

$$K = -3 \text{ or } K = -9$$

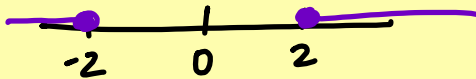
- 1) Isolate abs value
- 2) Write & solve 2 equations

$$|x| < 3$$



AND  
LESS THAN

$$|x| \geq 2$$



OR  
GREATER OR

$$4|6x+2| + 20 > 12$$

$$\frac{4|6x+2|}{4} > \frac{-8}{4}$$

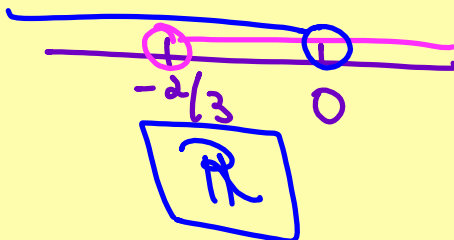
$$|6x+2| > -2$$

switch

$$6x+2 > -2 \quad \text{OR} \quad 6x+2 < -2$$

$$\frac{6x}{6} > \frac{-4}{6} \quad \frac{6x}{6} < \frac{-6}{6}$$

$$x > -\frac{2}{3} \quad x < -1$$



When isolated 1

$$|x+7| > -7$$

$\mathbb{R}$

$$|x+7| < -2$$

No solution

$$\begin{array}{rcl} -5|8-6x| & +45 & > -15 \\ & -45 & -45 \end{array}$$

$$\frac{-5|8-6x|}{-5} > \frac{-60}{-5}$$

$$|8 - 6x| < 12$$

$$8 - 6x < 12$$

$$-\frac{6x}{-6} < \frac{-48}{-6}$$

$$x > -2/3$$

$$8 - 6x > -12$$

$$\frac{20}{6} > \frac{6x}{6}$$

$$\frac{10}{3} > x$$

AND = overlap

$-2/3 < x < 10/3$

MATRIX - a rectangular array of numbers enclosed in brackets

$$\begin{bmatrix} 2 & -1 \\ 3 & 4 \\ 4 & 5 \end{bmatrix}$$

Dimensions: # of Rows  $\times$  # of Columns  
3  $\times$  2

$$\begin{bmatrix} 3 & -6 \\ 4 & 2 \\ 5 & -1 \end{bmatrix} + \begin{bmatrix} 8 & 0 \\ -9 & 3 \\ 3 & 7 \end{bmatrix} = \begin{bmatrix} 11 & -6 \\ -5 & 5 \\ 8 & 6 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 7 \\ -6 & 3 \end{bmatrix} + \begin{bmatrix} 5 & 6 \\ 8 & -2 \\ 9 & 1 \end{bmatrix} = \text{not possible}$$

$$\begin{aligned} & 3 \begin{bmatrix} 2 & 6 \\ 5 & -1 \end{bmatrix} - 2 \begin{bmatrix} 8 & 7 \\ 9 & -2 \end{bmatrix} \\ &= \begin{bmatrix} 6 & 18 \\ 15 & -3 \end{bmatrix} + \begin{bmatrix} -16 & -14 \\ -18 & 4 \end{bmatrix} \\ &= \begin{bmatrix} -10 & 4 \\ -3 & 1 \end{bmatrix} \end{aligned}$$

## Multiplication

$$\begin{bmatrix} \textcircled{3} & \textcircled{-2} & \textcircled{4} \\ \textcircled{1} & \textcircled{0} & \textcircled{-5} \end{bmatrix} \cdot \begin{bmatrix} \textcircled{5} & \textcircled{0} \\ \textcircled{-2} & \textcircled{6} \\ \textcircled{-1} & \textcircled{3} \end{bmatrix} = \begin{bmatrix} 15 + 4 + -4 & 0 + -12 + 12 \\ 5 + 0 + 5 & 0 + 0 + -15 \end{bmatrix}$$

$2 \times \textcircled{3}$        $\textcircled{3} \times 2$   
 possible

$$= \begin{bmatrix} 15 & 0 \\ 10 & -15 \end{bmatrix}$$

$2 \times 2$

#8) Find dimensions of the missing matrix:

$$[7 \times 9] * [9 \times 2] = ???$$

Answer:  $[7 \times 2]$  (If the inside dimensions are the same, the outside dimensions will be the size of the resulting matrix.)

#9) Calculator: P1 will do at beginning of next class.

P4 & B1: See video on website ([ncthunder.org/smeyer](http://ncthunder.org/smeyer))