

# LOGARITHMS - John Napier 1614

Exp  
form  $y = b^x$   
 $b > 0, b \neq 1$



Domain:  $(-\infty, \infty)$   
Range:  $(0, \infty)$

$$y = b^x$$

$$x = b^y$$

$$y = \log_b x$$

Domain:  $(0, \infty)$

Range:  $(-\infty, \infty)$

Common Logs

$$\log_{10} x = \log x$$

Natural Logs

$$\log_e x = \ln x$$

Logarithms are  
inverses of exponential  
functions.

Logs are used  
to solve for  
exponents!

$$2^3 = 8$$

$$y = \log(x-3)$$

Find domain:

Test plz!

~~3~~

$$(3, \infty)$$

$$\log_{12} 144 = \log_{12} 12^2 = 2$$

Make  
common  
bases!

$$\log_2 16 = \log_2 2^4 = 4$$

$$\log_9 \frac{1}{81} = \log_9 \frac{1}{9^2} = \log_9 9^{-2} = -2$$

$$\log_7 \sqrt[5]{7} = \log_7 7^{1/5} = \frac{1}{5}$$

$$\begin{aligned} \log_{11} \sqrt[3]{\frac{1}{121}} &= \log_{11} \sqrt[3]{\frac{1}{11^2}} \\ &= \log_{11} \sqrt[3]{11^{-2}} \\ &= \log_{11} 11^{-2/3} \\ &= -2/3 \end{aligned}$$

## Special Logs

### Common logs

$$\log_{10} x = \log x$$

### Natural logs

$$\log_e x = \ln x$$

$$\log 1000 = \log_{10} 10^3 = 3$$

$$\ln \sqrt[4]{e^7} = \ln e^{7/4} = \frac{7}{4}$$

$$8^{\log_8 50} = 50$$

$$e^{\ln 17} = 17$$

$$y = 2^x$$

$$y = \log_2 x$$

0	1
1	2
2	4
3	8

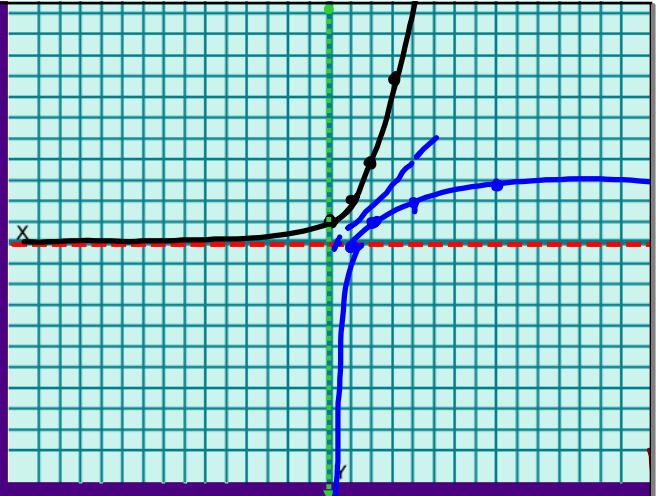
1	0
2	1
4	2
8	3

$$y = -\ln_e(x+4) + 2$$

1	0
2.7	-1
7.4	-2
3	

left  
4

up  
2



0

$$y = \log_2(x)$$

# SOLVING LOG EQUATIONS

Properties

$$\log_b m + \log_b n = \log_b(mn) \quad \log_7 x = 2$$

$$\log_b m - \log_b n = \log_b\left(\frac{m}{n}\right) \quad 7^{\log_7 x} = 7^2$$

$$\log_b m^p = p \cdot \log_b m$$

$$\boxed{x = 49}$$

Check!

$$\log_x 64 = 3$$

$$x^{\log_x 64} = x^3$$

$$\sqrt[3]{64} = \sqrt[3]{x^3}$$

$$\boxed{4 = x}$$

$$\log(x+3) - \log x = 1$$

$$\log_{10}\left(\frac{x+3}{x}\right) = 1$$

$$x \cdot \frac{x+3}{x} = 10 \cdot x$$

$$x+3 = 10x$$

$$3 = 9x$$

$$\frac{1}{3} = \frac{3}{9} = x$$

1) Use properties  
to reduce each  
side to one  
log

2) Exponentiate!

3) Check!